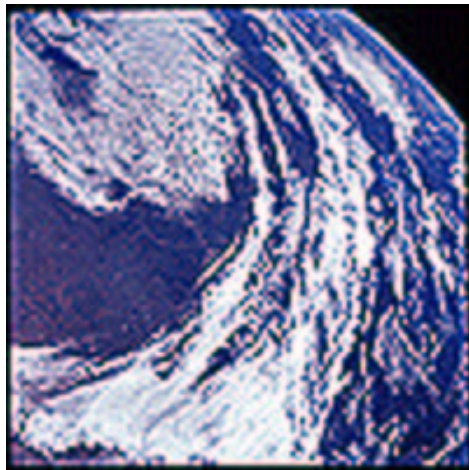


# Troposphere/Stratosphere Interaction

## A Simple Model

Katie Coughlin

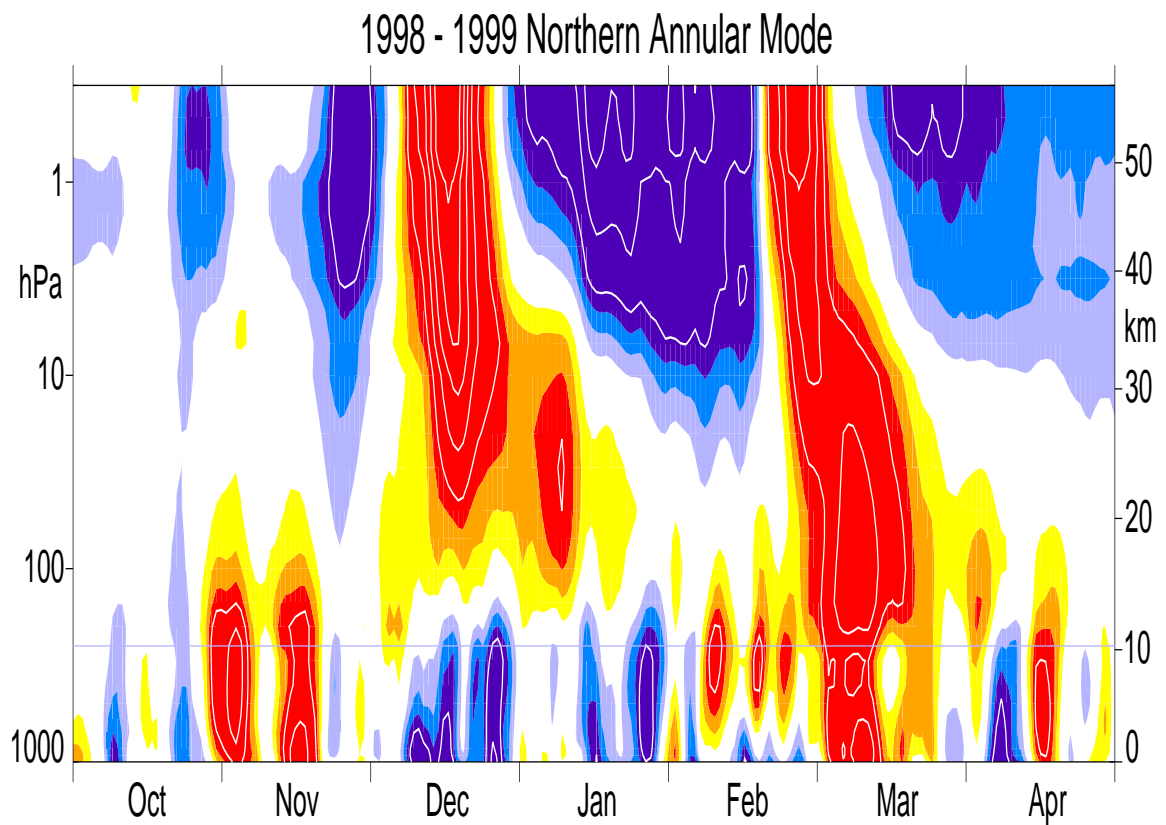


with Ka-Kit Tung  
*University of Washington*

## Overview

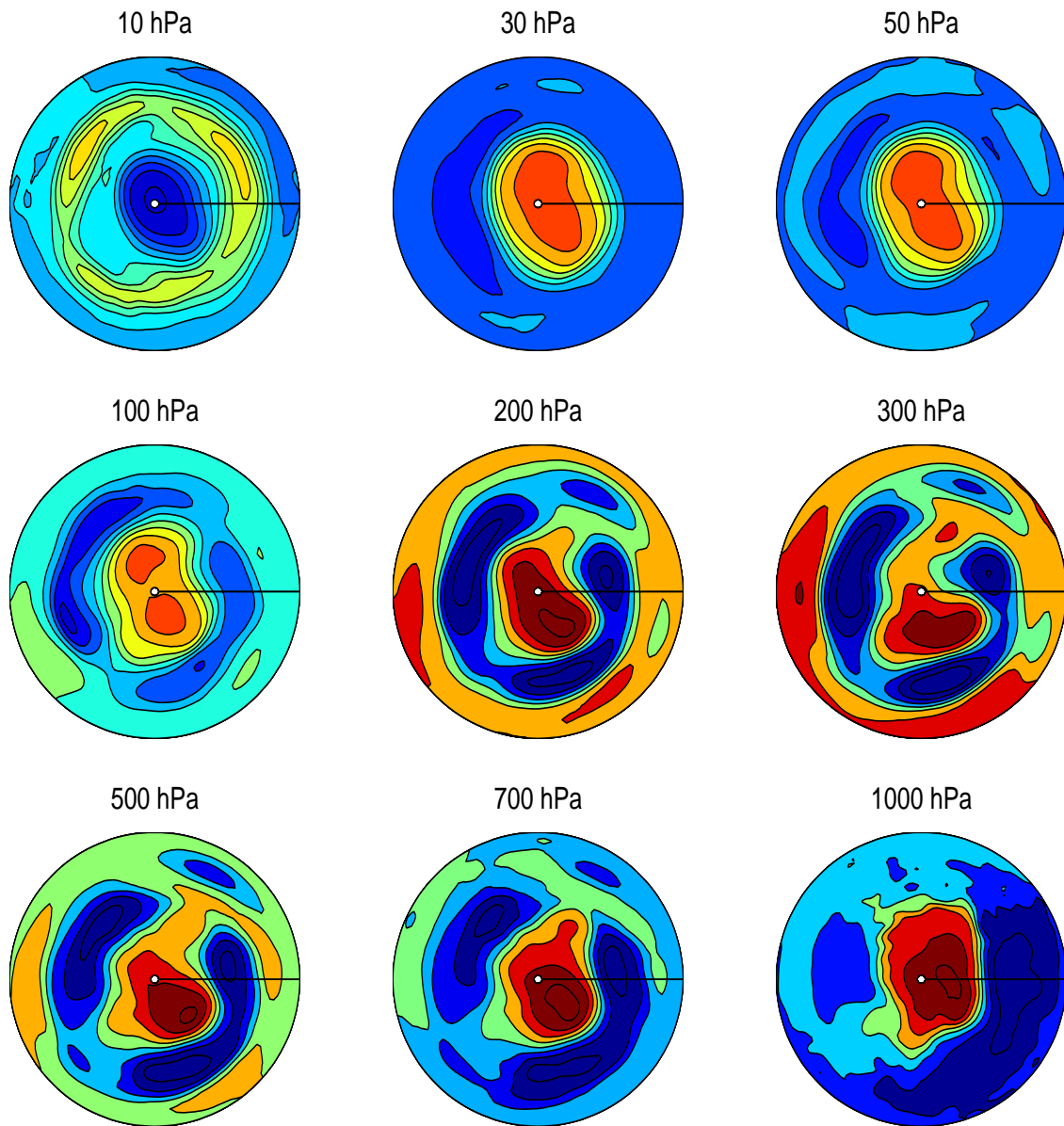
- Observations of zonal deceleration in the Stratosphere and the Wave Response in the Troposphere
- Explanation of the Simple Model
- Analytical Solutions show Tropospheric response to descending Stratospheric deceleration.

# Descent of Stratospheric Deceleration



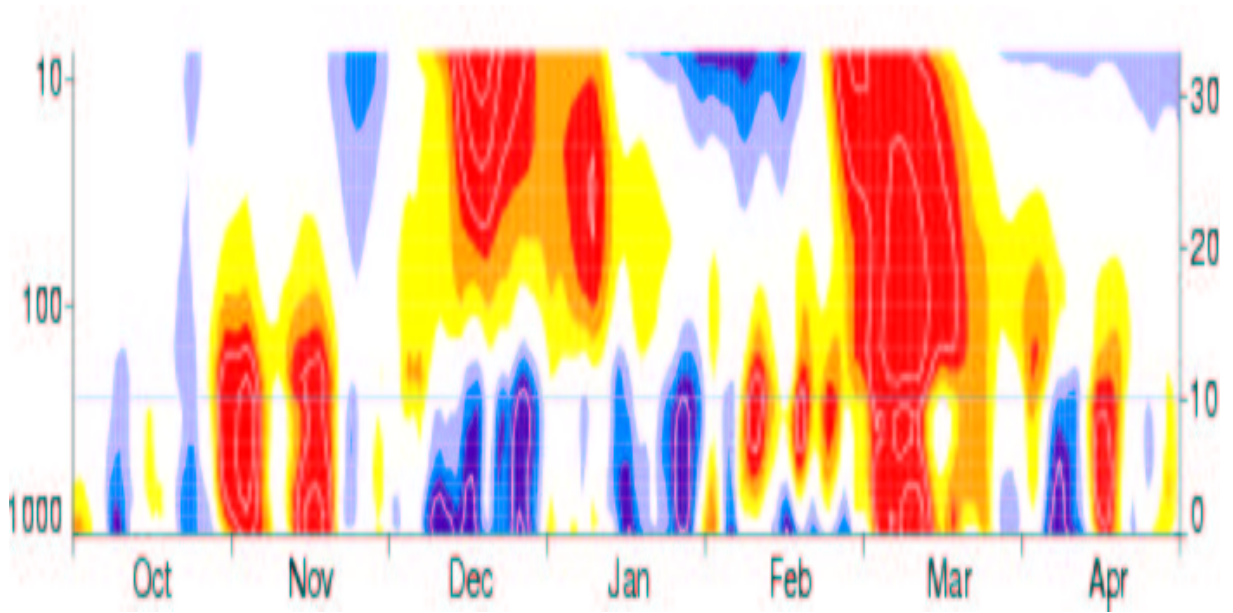
Baldwin, M.P., and T.J. Dunkerton, 2001: Stratospheric harbingers of anomalous weather regimes. *Science*, 294, 581-584.

## The Vertical Structures of the EOFs

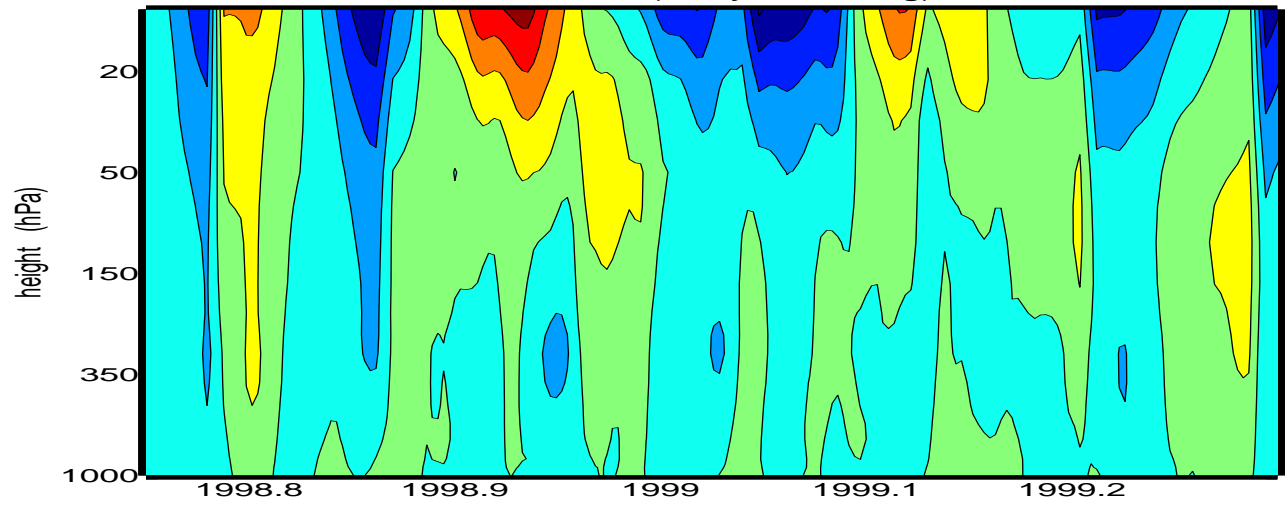


Winter EOFs from NOAA-CIRES Climate Diagnostic Center,  
Boulder CO.

## Zonal Mean is seen in the Stratosphere

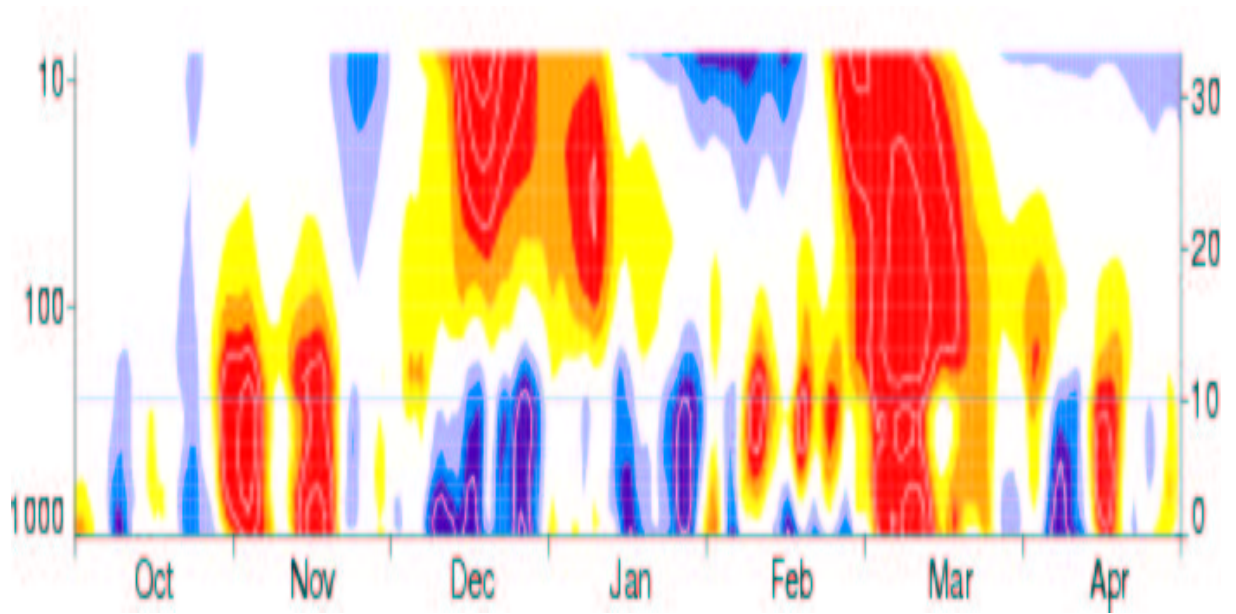


Zonal Mean (3 day smoothing)

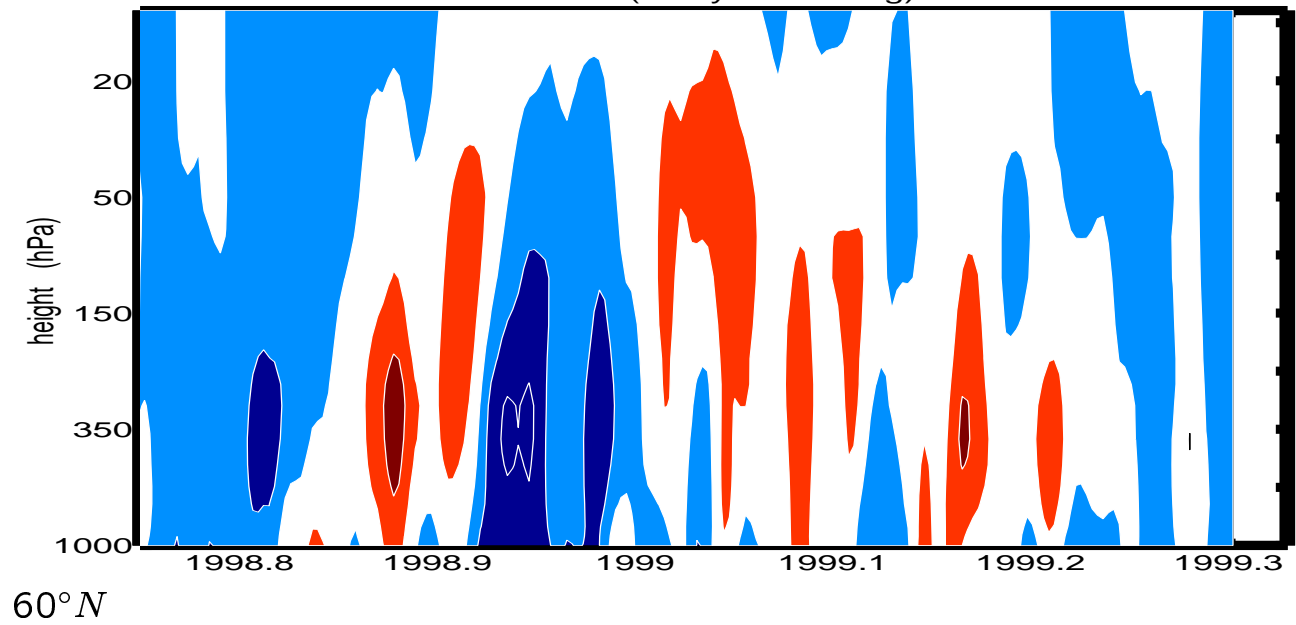


60°N

## Wave Reaction is seen in the Troposphere

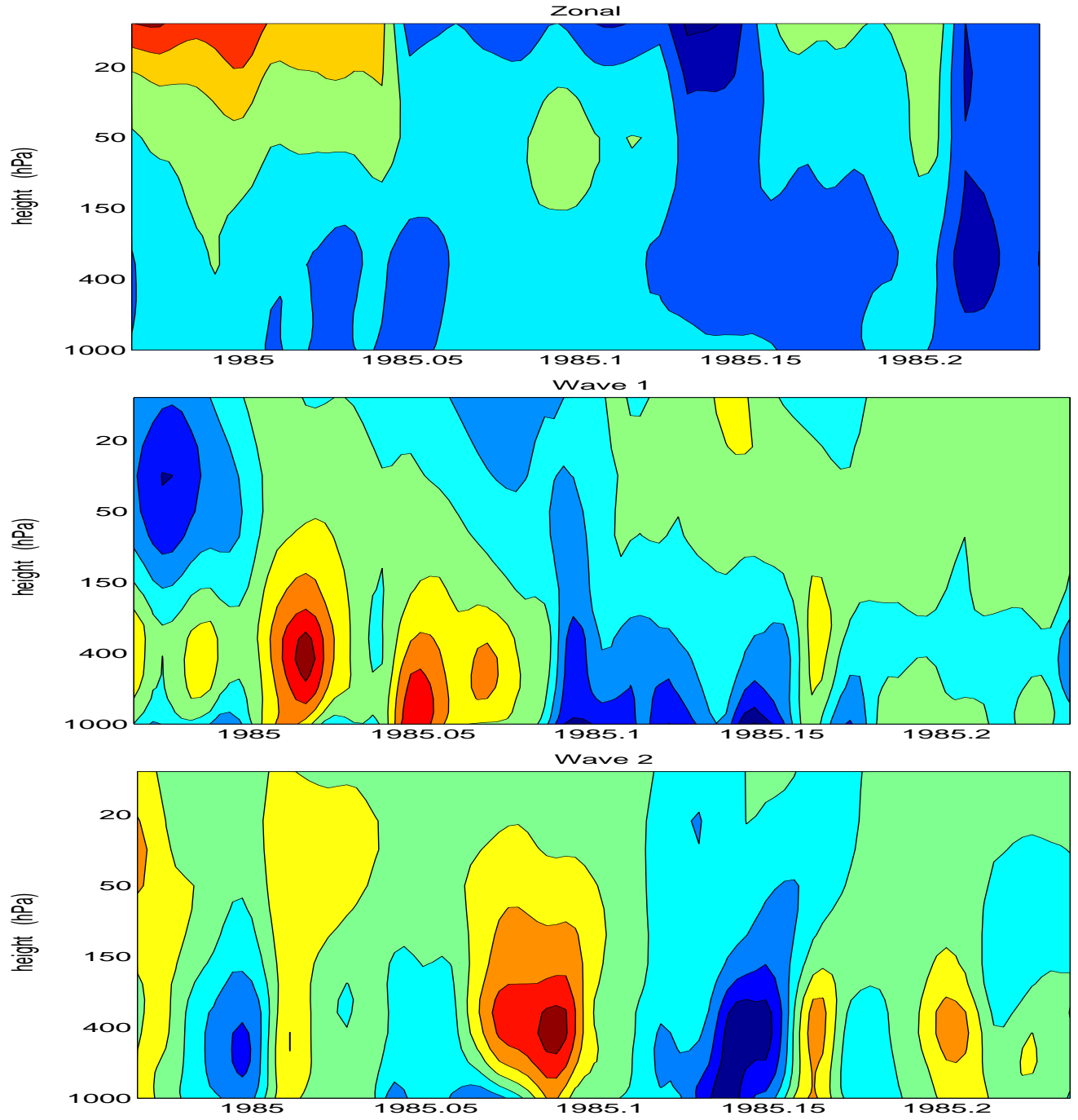


Wave 1 (3 day smoothing)



60°N

1985



60°N

## The Quasi-Geostrophic Equations

### Linearized Potential Vorticity

$$\epsilon(u_0 - c)(\Psi_{zz} - \Psi_z) + (u_0 - c)\Psi_{yy} + \Psi[-k^2(u_0 - c) - \epsilon(u_{0zz} - u_{0z}) + \beta] = 0$$

### Linearized Thermodynamics

$$\frac{-wN^2H}{ikf} + (c - u_0)\Psi_z + u_0\Psi = 0$$

$$\Psi(y, z) = \phi(y, z)e^{\frac{z}{H}}$$

$$\phi(y, z) = Y(y)Z(z)$$

$$F_* = -\frac{u_{0zz} - u_{0z}}{u_0 - c} + \frac{\beta}{\epsilon(u_0 - c)} - \frac{k^2 + l^2}{\epsilon} - \frac{1}{4}$$

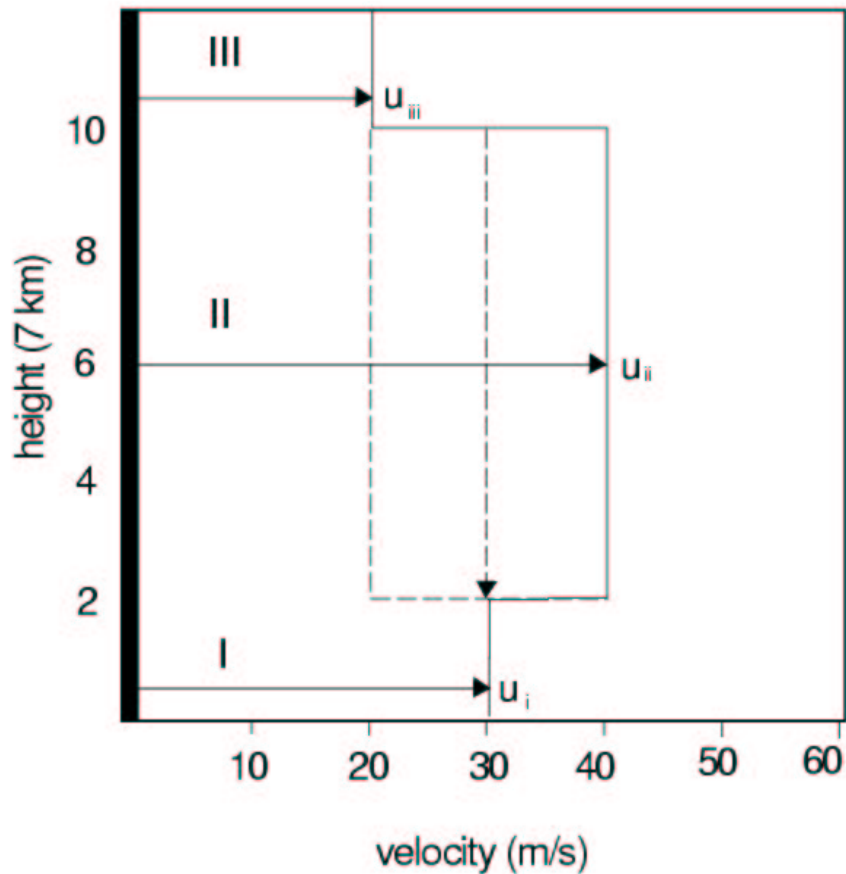
$$Y_{yy} + l^2Y = 0$$

$$Z_{zz} + F_*Z = 0$$

Assume  $c = 0$  and  $u_0(z)$ .



## Background Wind Speeds



## Boundary Conditions

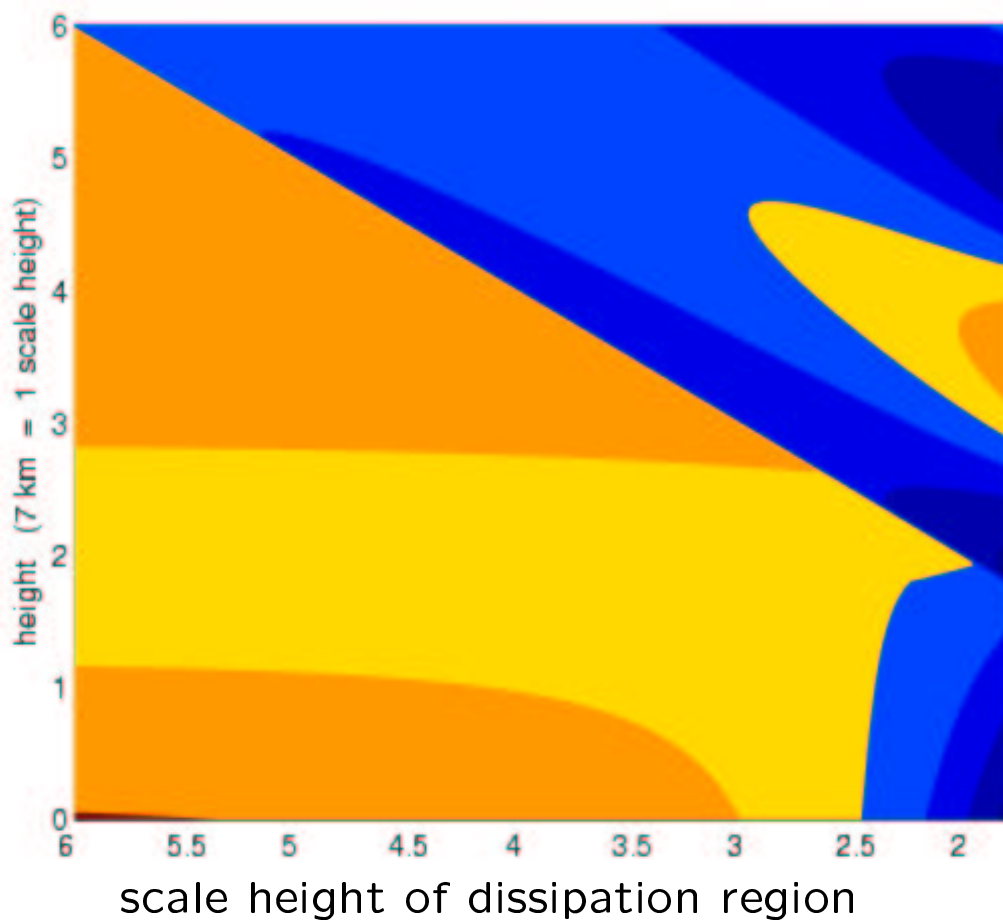
at the surface,  $z = 0$ ,  $w = u \frac{db}{dx}$

assume a Gaussian mountain  $\rightarrow b = e^{ikx} e^{-c^2(y - \frac{\pi a}{4})^2}$

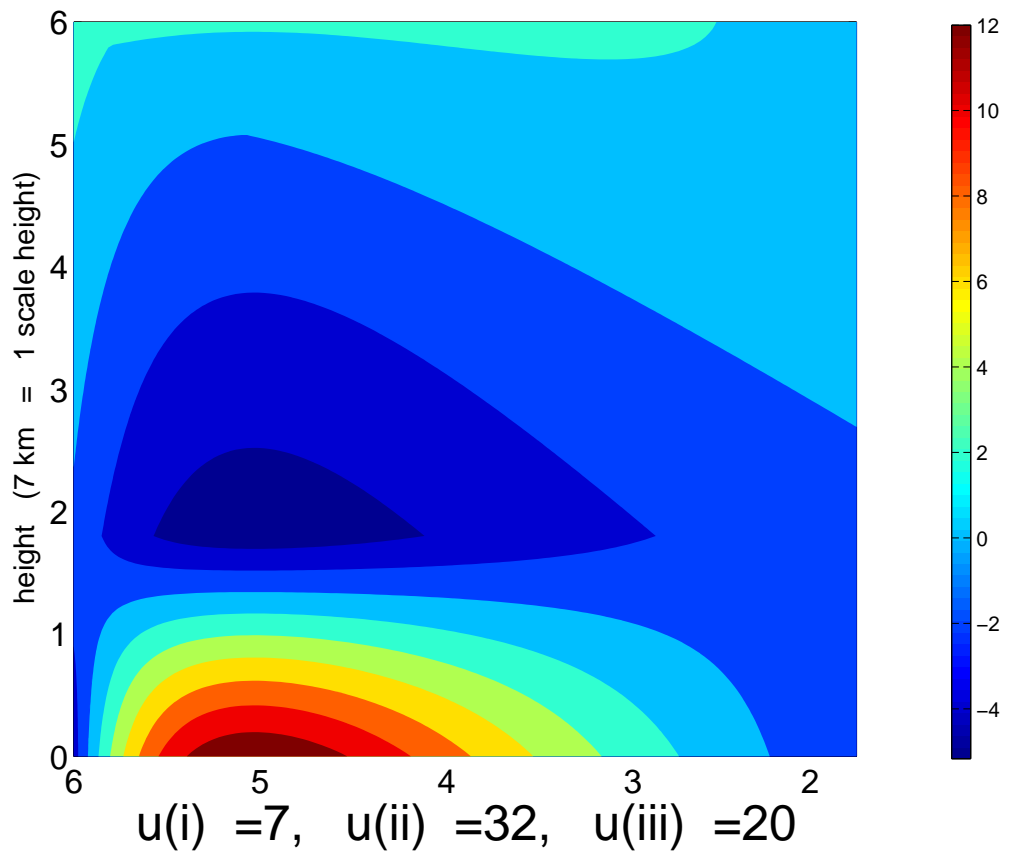
We require bounded solutions as our upper condition.  
 $\rightarrow$  vertical group velocity is positive.

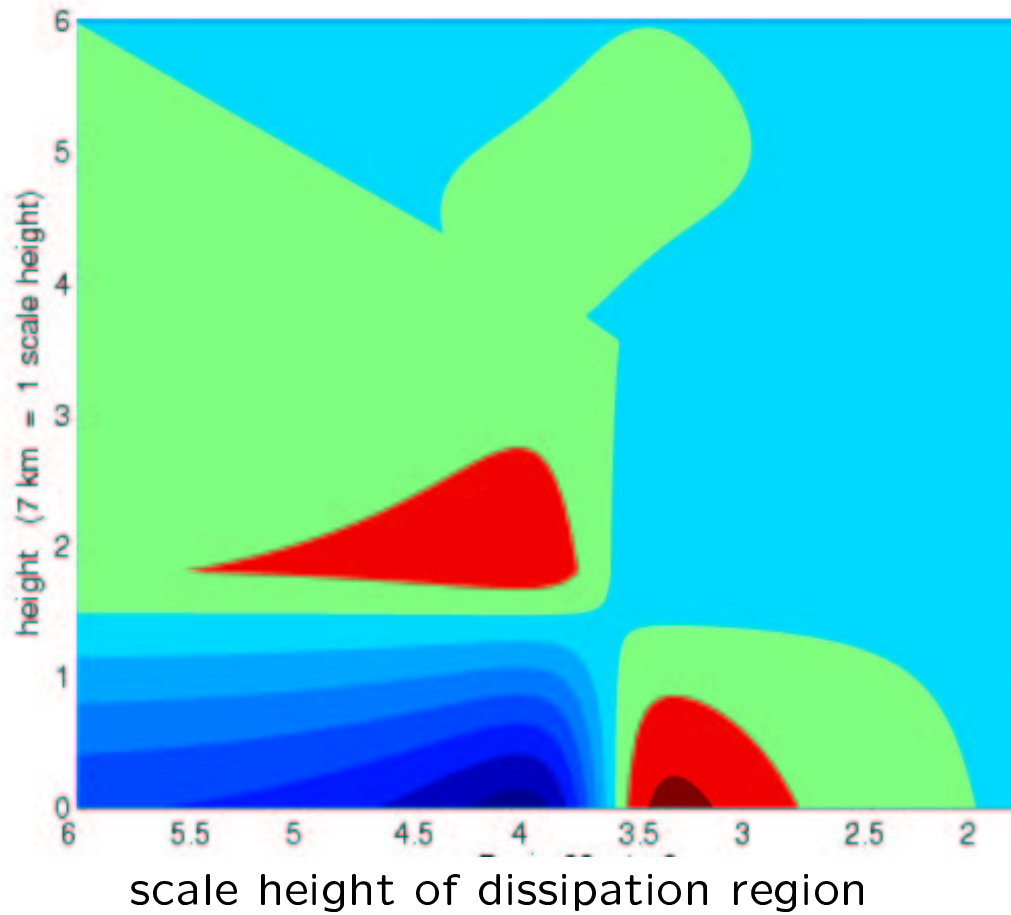
The vertical wave number is  $m = \pm \sqrt{-F_{top}}$  and the group velocity is  $c_g = \frac{d\omega}{dm}$ .

## Tropospheric Wave Reaction to Descending Deceleration



$$u_i = 17 \text{ m/s}, u_{ii} = 50 \text{ m/s}, u_{iii} = 4 \text{ m/s}$$





$$u_i = 7 \text{ m/s}, u_{ii} = 60 \text{ m/s}, u_{iii} = 9 \text{ m/s}$$

## Conclusions

Tropospheric Waves respond to Stratospheric changes in zonal wind speed (i.e. stratospheric changes in the index of refraction).